

## A-Level Maths - Integration (Year 1)

1. Find

$$\int \left( 2x^5 - \frac{1}{4x^3} - 5 \right) dx$$

giving each term in its simplest form.

*Edexcel Core 1 Paper, June 2017*

2. Find

$$\int \left( 10x^4 - 4x - \frac{3}{\sqrt{x}} \right) dx$$

giving each term in its simplest form.

*Edexcel Core 1 Paper, June 2013*

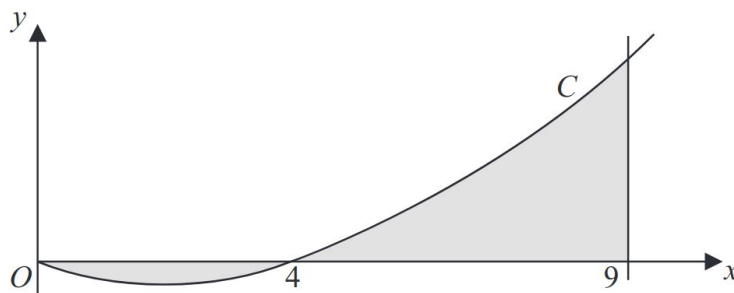
3.

(a) Find

$$\int 10x(x^{\frac{1}{2}} - 2) dx$$

giving each term in its simplest form.

**(4)**



**Figure 2**

Figure 2 shows a sketch of part of the curve  $C$  with equation

$$y = 10x(x^{\frac{1}{2}} - 2), \quad x \geq 0$$

The curve  $C$  starts at the origin and crosses the  $x$ -axis at the point  $(4, 0)$ .

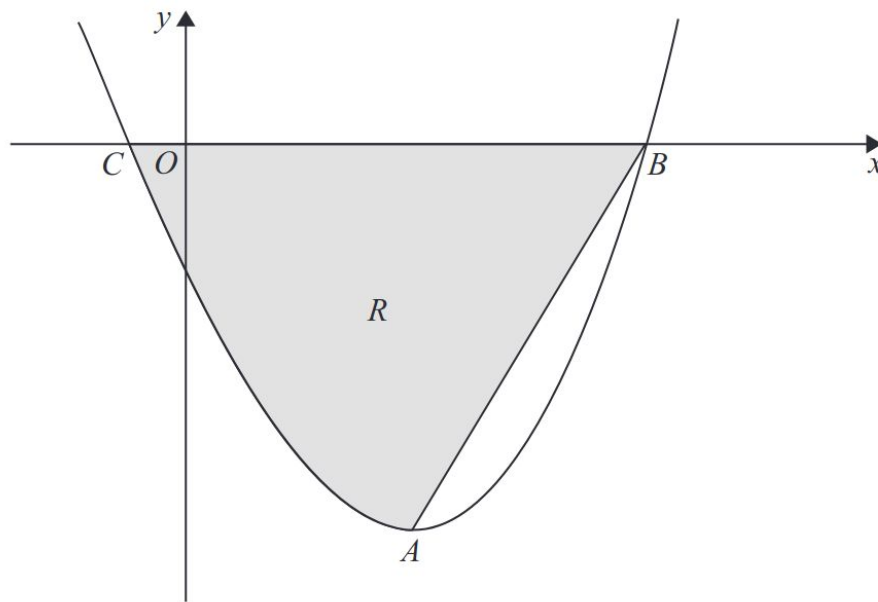
The area, shown shaded in Figure 2, consists of two finite regions and is bounded by the curve  $C$ , the  $x$ -axis and the line  $x = 9$

(b) Use your answer from part (a) to find the total area of the shaded regions.

**(5)**

*Edexcel Core 2 Paper, June 2015*

4.



**Figure 2**

Figure 2 shows a sketch of part of the curve with equation

$$y = 4x^3 + 9x^2 - 30x - 8, \quad -0.5 \leq x \leq 2.2$$

The curve has a turning point at the point  $A$ .

(a) Using calculus, show that the  $x$  coordinate of  $A$  is 1

**(3)**

The curve crosses the  $x$ -axis at the points  $B(2, 0)$  and  $C\left(-\frac{1}{4}, 0\right)$

The finite region  $R$ , shown shaded in Figure 2, is bounded by the curve, the line  $AB$ , and the  $x$ -axis.

(b) Use integration to find the area of the finite region  $R$ , giving your answer to 2 decimal places.

**(7)**